

## 07 - Age analysis

Xiaoyue Xi and Oliver Ratmann

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This vignette provides an extension of the general method of **phyloflow**. The aim is to understand the transmission flows between one-year increment age groups. The differences between this example with the general pipeline of **phyloflow** is the correlation between flows. To tackle this problem, we impose a Gaussian process (GP) prior on transmission flows. Also, a more flexible platform, Stan, is introduced to solve the problem.

### Dataset

We start with simulating transmission counts between seven age groups called “15-19”, “20-24”, “25-29”, “30-34”, “35-39”, “40-44”, “45-49”. Note that in practice, it would be good to use this method to investigate transmission dynamics between one-year increment age group, as the squared exponential kernel is for the continuous input space. We first set up hyperparameters for GP, the baseline and sampling fractions.

```
library(rstan)
library(data.table)
library(ggplot2)
library(viridis)
library(phyloflows)
set.seed(42)
rstan_options(auto_write = TRUE)
options(mc.cores = parallel::detectCores())
alpha_true <- c(2.5)
rho_true <- c(12,9)
mu_true <- -1
gp_dim <- 2
xi <- c(0.35, 0.45, 0.5, 0.55, 0.5, 0.55, 0.4)
```

Next, we calculate the sampling probabilities of transmission flows within and between the two groups.

```
dobs <- data.table(expand.grid(TR_TRM_CATEGORY = c("15-19", "20-24", "25-29", "30-34", "35-39", "40-44", "45-49"),
                             REC_TRM_CATEGORY = c("15-19", "20-24", "25-29", "30-34", "35-39", "40-44", "45-49")))
```

```
ds <- data.table(CATEGORY = c("15-19", "20-24", "25-29",
                             "30-34", "35-39", "40-44", "45-49"),
                P = xi, ID = 1:7)
```

```
setnames(ds, colnames(ds), paste0('TR_TRM_', colnames(ds)))
dobs <- merge(dobs, ds, by='TR_TRM_CATEGORY')
setnames(ds, colnames(ds), gsub('TR_', 'REC_', colnames(ds)))
dobs <- merge(dobs, ds, by='REC_TRM_CATEGORY')
setnames(ds, colnames(ds), gsub('REC_TRM_', '', colnames(ds)))
dobs[, P:= TR_TRM_P * REC_TRM_P]
dobs[, TR_SMOOTH_CATEGORY:=as.numeric(substr(TR_TRM_CATEGORY, 1, 2))+2]
```

```
dobs[,REC_SMOOTH_CATEGORY:=as.numeric(substr(REC_TRM_CATEGORY,1,2))+2]
dobs[, TR_SAMPLING_CATEGORY:= TR_TRM_CATEGORY]
dobs[, REC_SAMPLING_CATEGORY:= REC_TRM_CATEGORY]
```

Then we simulate true transmission flows and observed transmission counts.

```
simu_pars <- list( N=nrow(dobs), D=gp_dim, x=cbind(dobs$TR_SMOOTH_CATEGORY,dobs$REC_SMOOTH_CATEGORY),
                  alpha=alpha_true, rho=rho_true,
                  mu=mu_true,xi=dobs$P)
# simulate data set
simu_fit <- stan( file="simu_poiss.stan",
                  data=simu_pars, iter=1,
                  chains=1, seed=424838, algorithm="Fixed_param")
dobs$TRM_OBS <- extract(simu_fit)$y[1,]
```

The data can be loaded through

```
data(sevenGroupFlows1,package='phyloflows')
```

## Input data: observed transmission flows

Input data of the similar format of **phyloflow** are expected.

```
dobs <- subset(dobs, select = c('TR_TRM_CATEGORY', 'REC_TRM_CATEGORY', 'TR_SAMPLING_CATEGORY',
                               'REC_SAMPLING_CATEGORY', 'TR_SMOOTH_CATEGORY', 'REC_SMOOTH_CATEGORY',
                               'TRM_OBS'))
```

```
head(dobs)
```

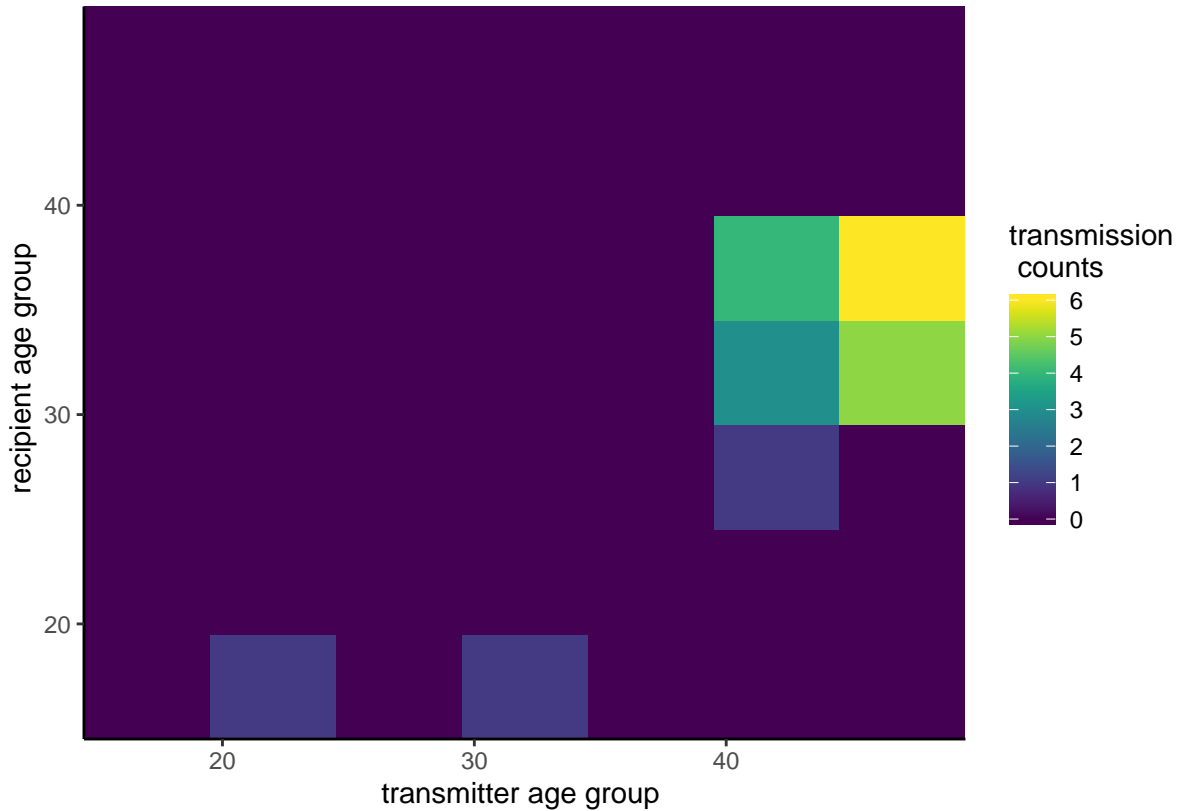
	TR_TRM_CATEGORY	REC_TRM_CATEGORY	TR_SAMPLING_CATEGORY	REC_SAMPLING_CATEGORY	TR_SMOOTH_CATEGORY	REC_SMOOTH_CATEGORY	TRM_OBS
#> 1:	15-19	15-19	15-19	15-19	15-19	15-19	0
#> 2:	20-24	15-19	20-24	15-19	15-19	15-19	1
#> 3:	25-29	15-19	25-29	15-19	15-19	15-19	0
#> 4:	30-34	15-19	30-34	15-19	15-19	15-19	1
#> 5:	35-39	15-19	35-39	15-19	15-19	15-19	0
#> 6:	40-44	15-19	40-44	15-19	15-19	15-19	0

**dobs** specifies observed counts of transmissions from a transmitter age group to a recipient age group. It must contain the following columns:

- *TR\_TRM\_CATEGORY* name of transmitter group.
- *REC\_TRM\_CATEGORY* name of recipient group.
- *TR\_SMOOTH\_CATEGORY* midpoint of transmitter age group.
- *REC\_SMOOTH\_CATEGORY* midpoint of recipient age group.
- *TRM\_CAT\_PAIR\_ID* identifier of transmitter-recipient pair
- *TRM\_OBS* observed transmission counts

Let us look at the data. The first row shows zero counts of transmission flows from age group “15-19” to age group “15-19”. We visualise our simulated input data in the heatmap :

```
ggplot(dobs, aes(TR_SMOOTH_CATEGORY, REC_SMOOTH_CATEGORY))+
  geom_tile(aes(fill = TRM_OBS)) +
  scale_fill_viridis() +
  scale_x_continuous(expand = c(0,0), limits = c(14.5,49.5))+
  scale_y_continuous(expand = c(0,0), limits = c(14.5,49.5))+
  theme_classic()+
  labs(x='transmitter age group \n', y='\n recipient age group',fill='transmission \n counts')
```



## Input data: sampling information

`dobs` also requires information about how each group was sampled. This is stored in the following columns:

- `TR_SAMPLING_CATEGORY` sampling strata of transmitter group
- `REC_SAMPLING_CATEGORY` sampling strata of recipient group

`dprior.fit` specifies the distribution of sampling probability in each sampling group. The sampling probability is either characterised by beta-binomial model or GLM model (See 01 - Simulating data). and given in the form of samples. In the tutorial, we opted for a probabilistic programming language Stan, and it cannot take samples as input. However, it is possible to fit statistical distributions to samples and input distribution parameters. The information is stored in data `dprior.fit` in the following columns:

- `SAMPLING_CATEGORY` name of sampling strata
- `ALPHA`, `BETA` shape parameters of the distribution of sampling probability.

Under beta-binomial model, the posterior distribution of the sampling probability is known analytically, i.e. beta. Let us look at the sampling information:

```

ds$TRIAL <- c(4000, 3700, 3300, 2500, 1700, 1000, 500)
ds[,SUC := round(TRIAL * P)]
dprior.fit <- copy(ds)
dprior.fit[,ALPHA := SUC+1]
dprior.fit[,BETA := TRIAL-SUC+1]
dprior.fit <- subset(dprior.fit, select = c('CATEGORY','ALPHA','BETA'))
colnames(dprior.fit) <- c('SAMPLING_CATEGORY','ALPHA','BETA')
head(dprior.fit)
#>   SAMPLING_CATEGORY ALPHA BETA
#> 1:                15-19  1401 2601
#> 2:                20-24  1666 2036
#> 3:                25-29  1651 1651
#> 4:                30-34  1376 1126
#> 5:                35-39   851   851
#> 6:                40-44   551   451

```

## Method

Again we use a Bayesian approach to estimate the proportion of transmissions between the two population groups. Please see the problem setting in **phyloflows: Estimating transmission flows under heterogeneous sampling – a first example**. Unlike the simple example, a probabilistic programming language Stan provides a flexible platform to impose different kinds of priors. Recall the posterior distribution of the parameters  $(\lambda, s)$  is given by

$$\begin{aligned}
p(\lambda, s|n) &\propto p(n|\lambda, s)p(\lambda, s) \\
&= \prod_{i=1, \dots, 7; j=1, \dots, 7} \text{Poisson}(n_{ij}; \lambda_{ij} * s_i * s_j) p(\lambda_{ij}) p(s_i) p(s_j).
\end{aligned}$$

Then, we calculate the main quantity of interest,  $\pi$ , via

$$\pi_{ij} = \lambda_{ij} / \sum_{k=1, \dots, 7; l=1, \dots, 7} \lambda_{kl}.$$

for  $i = 1, \dots, 7$  and  $j = 1, \dots, 7$ .

**For the prior distributions**, we specify for  $p(\lambda_{ij})$ ,  $i = 1, 2; j = 1, 2$  uninformative prior distributions. We use a Gamma distribution with parameters  $\alpha_i = 0.8/7^2$  and  $\beta = 0.8/Z$  with  $Z = \sum_{ij|n_{ij}>0} n_{ij}/(s_i * s_j) + \sum_{ij|n_{ij}>0} (1 - s_i * s_j)/(s_i * s_j)$ . This choice implies for  $\pi$  a Dirichlet prior distribution with parameters  $\alpha_i$ , which is considered to be an objective choice. For  $p(s_i)$ , we use a strongly informative prior distribution, based on the available data as illustrated above.

An alternative prior distribution is Gaussian process prior, which penalises large changes between neighbouring age groups, and the kernel  $k$  is given by

$$k((a, b), (a', b')) = \sigma^2 \exp(-0.5((\frac{a - a'}{\ell_1})^2 + (\frac{b - b'}{\ell_2})^2))$$

That is,  $\lambda_{ij} = \mu + f$  where  $f \sim \mathcal{GP}(0, k)$ .

## MCMC

### MCMC syntax

We use a Markov Chain Monte Carlo algorithm to sample from the posterior. The syntax for running the algorithm is as follows.

```

# specify a list of control variables:
# seed      random number seed
# mcmc.n    number of MCMC iterations
# method "gamma" or "gp"
# outfile output file name if you like to have the results
#          written to an *.rda* file
control <- list(seed=42, mcmc.n=500, method='gamma')
# run MCMC
ans.gamma <- source.attribution.mcmc.stan(dobs, dprior.fit, control)
# save(ans.gamma, file = '~/phyloscanner/phyloflows/data/sevenGroupFlows1_gamma_mcmc.RData')

control <- list(seed=42, mcmc.n=500, method='gp')
# run MCMC
ans.gp <- source.attribution.mcmc.stan(dobs, dprior.fit, control)
# save(ans.gp, file = '~/phyloscanner/phyloflows/data/sevenGroupFlows1_gp_mcmc.RData')

```

## MCMC output

Let us have a look at the output:

```

str(ans.gamma)
#> Formal class 'stanfit' [package "rstan"] with 10 slots
#> ..@ model_name: chr "gamma"
#> ..@ model_pars: chr [1:6] "lambda" "xi" "lxi_pair" "betav" ...
#> ..@ par_dims :List of 6
#> .. ..$ lambda : num 49
#> .. ..$ xi      : num 7
#> .. ..$ lxi_pair: num 49
#> .. ..$ betav   : num 49
#> .. ..$ beta    : num(0)
#> .. ..$ lp__    : num(0)
#> ..@ mode      : int 0
#> ..@ sim       :List of 12
#> .. ..$ samples :List of 1
#> .. .. ..$ :List of 156
#> .. .. ..$ lambda[1] : num [1:500] 0.00883 0.00883 0.00883 0.00883 0.00946 ...
#> .. .. ..$ lambda[2] : num [1:500] 0.697 0.697 0.697 0.697 0.694 ...
#> .. .. ..$ lambda[3] : num [1:500] 0.07 0.07 0.07 0.07 0.0693 ...
#> .. .. ..$ lambda[4] : num [1:500] 7.09 7.09 7.09 7.09 6.87 ...
#> .. .. ..$ lambda[5] : num [1:500] 0.124 0.124 0.124 0.124 0.121 ...
#> .. .. ..$ lambda[6] : num [1:500] 0.0621 0.0621 0.0621 0.0621 0.0625 ...
#> .. .. ..$ lambda[7] : num [1:500] 2.86e-05 2.86e-05 2.86e-05 2.86e-05 2.71e-05 ...
#> .. .. ..$ lambda[8] : num [1:500] 0.281 0.281 0.281 0.281 0.281 ...
#> .. .. ..$ lambda[9] : num [1:500] 0.0357 0.0357 0.0357 0.0357 0.0354 ...
#> .. .. ..$ lambda[10] : num [1:500] 0.0446 0.0446 0.0446 0.0446 0.0451 ...
#> .. .. ..$ lambda[11] : num [1:500] 0.857 0.857 0.857 0.857 0.93 ...
#> .. .. ..$ lambda[12] : num [1:500] 0.0186 0.0186 0.0186 0.0186 0.0185 ...
#> .. .. ..$ lambda[13] : num [1:500] 0.000392 0.000392 0.000392 0.000392 0.000387 ...
#> .. .. ..$ lambda[14] : num [1:500] 0.00137 0.00137 0.00137 0.00137 0.00135 ...
#> .. .. ..$ lambda[15] : num [1:500] 0.666 0.666 0.666 0.666 0.609 ...
#> .. .. ..$ lambda[16] : num [1:500] 0.0176 0.0176 0.0176 0.0176 0.0175 ...
#> .. .. ..$ lambda[17] : num [1:500] 0.0438 0.0438 0.0438 0.0438 0.0425 ...
#> .. .. ..$ lambda[18] : num [1:500] 0.033 0.033 0.033 0.033 0.0355 ...
#> .. .. ..$ lambda[19] : num [1:500] 0.142 0.142 0.142 0.142 0.14 ...

```

```

#> .. .. .. ..$ lambda[20] : num [1:500] 2.94 2.94 2.94 2.94 2.9 ...
#> .. .. .. ..$ lambda[21] : num [1:500] 0.391 0.391 0.391 0.391 0.354 ...
#> .. .. .. ..$ lambda[22] : num [1:500] 0.671 0.671 0.671 0.671 0.659 ...
#> .. .. .. ..$ lambda[23] : num [1:500] 1.17 1.17 1.17 1.17 1.06 ...
#> .. .. .. ..$ lambda[24] : num [1:500] 0.0741 0.0741 0.0741 0.0741 0.0775 ...
#> .. .. .. ..$ lambda[25] : num [1:500] 0.00197 0.00197 0.00197 0.00197 0.00191 ...
#> .. .. .. ..$ lambda[26] : num [1:500] 0.124 0.124 0.124 0.124 0.126 ...
#> .. .. .. ..$ lambda[27] : num [1:500] 7.29 7.29 7.29 7.29 6.91 ...
#> .. .. .. ..$ lambda[28] : num [1:500] 0.078 0.078 0.078 0.078 0.0768 ...
#> .. .. .. ..$ lambda[29] : num [1:500] 0.0512 0.0512 0.0512 0.0512 0.0497 ...
#> .. .. .. ..$ lambda[30] : num [1:500] 0.321 0.321 0.321 0.321 0.328 ...
#> .. .. .. ..$ lambda[31] : num [1:500] 0.0196 0.0196 0.0196 0.0196 0.0187 ...
#> .. .. .. ..$ lambda[32] : num [1:500] 0.00496 0.00496 0.00496 0.00496 0.00467 ...
#> .. .. .. ..$ lambda[33] : num [1:500] 0.0136 0.0136 0.0136 0.0136 0.0133 ...
#> .. .. .. ..$ lambda[34] : num [1:500] 0.131 0.131 0.131 0.131 0.135 ...
#> .. .. .. ..$ lambda[35] : num [1:500] 8.02 8.02 8.02 8.02 8.04 ...
#> .. .. .. ..$ lambda[36] : num [1:500] 0.731 0.731 0.731 0.731 0.778 ...
#> .. .. .. ..$ lambda[37] : num [1:500] 0.38 0.38 0.38 0.38 0.347 ...
#> .. .. .. ..$ lambda[38] : num [1:500] 0.000202 0.000202 0.000202 0.000202 0.000205 ...
#> .. .. .. ..$ lambda[39] : num [1:500] 0.00875 0.00875 0.00875 0.00875 0.00957 ...
#> .. .. .. ..$ lambda[40] : num [1:500] 0.00122 0.00122 0.00122 0.00122 0.00132 ...
#> .. .. .. ..$ lambda[41] : num [1:500] 1.24 1.24 1.24 1.24 1.22 ...
#> .. .. .. ..$ lambda[42] : num [1:500] 0.0574 0.0574 0.0574 0.0574 0.0569 ...
#> .. .. .. ..$ lambda[43] : num [1:500] 0.0333 0.0333 0.0333 0.0333 0.0357 ...
#> .. .. .. ..$ lambda[44] : num [1:500] 0.176 0.176 0.176 0.176 0.164 ...
#> .. .. .. ..$ lambda[45] : num [1:500] 0.026 0.026 0.026 0.026 0.0257 ...
#> .. .. .. ..$ lambda[46] : num [1:500] 0.00561 0.00561 0.00561 0.00561 0.00529 ...
#> .. .. .. ..$ lambda[47] : num [1:500] 0.000297 0.000297 0.000297 0.000297 0.00031 ...
#> .. .. .. ..$ lambda[48] : num [1:500] 0.291 0.291 0.291 0.291 0.293 ...
#> .. .. .. ..$ lambda[49] : num [1:500] 0.000651 0.000651 0.000651 0.000651 0.000661 ...
#> .. .. .. ..$ xi[1] : num [1:500] 0.118 0.118 0.118 0.118 0.202 ...
#> .. .. .. ..$ xi[2] : num [1:500] 0.51 0.51 0.51 0.51 0.48 ...
#> .. .. .. ..$ xi[3] : num [1:500] 0.609 0.609 0.609 0.609 0.561 ...
#> .. .. .. ..$ xi[4] : num [1:500] 0.543 0.543 0.543 0.543 0.557 ...
#> .. .. .. ..$ xi[5] : num [1:500] 0.432 0.432 0.432 0.432 0.46 ...
#> .. .. .. ..$ xi[6] : num [1:500] 0.644 0.644 0.644 0.644 0.617 ...
#> .. .. .. ..$ xi[7] : num [1:500] 0.241 0.241 0.241 0.241 0.247 ...
#> .. .. .. ..$ lxi_pair[1] : num [1:500] -4.27 -4.27 -4.27 -4.27 -3.2 ...
#> .. .. .. ..$ lxi_pair[2] : num [1:500] -2.81 -2.81 -2.81 -2.81 -2.34 ...
#> .. .. .. ..$ lxi_pair[3] : num [1:500] -2.63 -2.63 -2.63 -2.63 -2.18 ...
#> .. .. .. ..$ lxi_pair[4] : num [1:500] -2.74 -2.74 -2.74 -2.74 -2.19 ...
#> .. .. .. ..$ lxi_pair[5] : num [1:500] -2.97 -2.97 -2.97 -2.97 -2.38 ...
#> .. .. .. ..$ lxi_pair[6] : num [1:500] -2.57 -2.57 -2.57 -2.57 -2.08 ...
#> .. .. .. ..$ lxi_pair[7] : num [1:500] -3.56 -3.56 -3.56 -3.56 -3 ...
#> .. .. .. ..$ lxi_pair[8] : num [1:500] -2.81 -2.81 -2.81 -2.81 -2.34 ...
#> .. .. .. ..$ lxi_pair[9] : num [1:500] -1.35 -1.35 -1.35 -1.35 -1.47 ...
#> .. .. .. ..$ lxi_pair[10] : num [1:500] -1.17 -1.17 -1.17 -1.17 -1.31 ...
#> .. .. .. ..$ lxi_pair[11] : num [1:500] -1.28 -1.28 -1.28 -1.28 -1.32 ...
#> .. .. .. ..$ lxi_pair[12] : num [1:500] -1.51 -1.51 -1.51 -1.51 -1.51 ...
#> .. .. .. ..$ lxi_pair[13] : num [1:500] -1.11 -1.11 -1.11 -1.11 -1.22 ...
#> .. .. .. ..$ lxi_pair[14] : num [1:500] -2.1 -2.1 -2.1 -2.1 -2.13 ...
#> .. .. .. ..$ lxi_pair[15] : num [1:500] -2.63 -2.63 -2.63 -2.63 -2.18 ...
#> .. .. .. ..$ lxi_pair[16] : num [1:500] -1.17 -1.17 -1.17 -1.17 -1.31 ...

```

```

#> .. .. .. ..$ lxi_pair[17]: num [1:500] -0.993 -0.993 -0.993 -0.993 -1.156 ...
#> .. .. .. ..$ lxi_pair[18]: num [1:500] -1.11 -1.11 -1.11 -1.11 -1.16 ...
#> .. .. .. ..$ lxi_pair[19]: num [1:500] -1.34 -1.34 -1.34 -1.34 -1.35 ...
#> .. .. .. ..$ lxi_pair[20]: num [1:500] -0.937 -0.937 -0.937 -0.937 -1.06 ...
#> .. .. .. ..$ lxi_pair[21]: num [1:500] -1.92 -1.92 -1.92 -1.92 -1.98 ...
#> .. .. .. ..$ lxi_pair[22]: num [1:500] -2.74 -2.74 -2.74 -2.74 -2.19 ...
#> .. .. .. ..$ lxi_pair[23]: num [1:500] -1.28 -1.28 -1.28 -1.28 -1.32 ...
#> .. .. .. ..$ lxi_pair[24]: num [1:500] -1.11 -1.11 -1.11 -1.11 -1.16 ...
#> .. .. .. ..$ lxi_pair[25]: num [1:500] -1.22 -1.22 -1.22 -1.22 -1.17 ...
#> .. .. .. ..$ lxi_pair[26]: num [1:500] -1.45 -1.45 -1.45 -1.45 -1.36 ...
#> .. .. .. ..$ lxi_pair[27]: num [1:500] -1.05 -1.05 -1.05 -1.05 -1.07 ...
#> .. .. .. ..$ lxi_pair[28]: num [1:500] -2.03 -2.03 -2.03 -2.03 -1.99 ...
#> .. .. .. ..$ lxi_pair[29]: num [1:500] -2.97 -2.97 -2.97 -2.97 -2.38 ...
#> .. .. .. ..$ lxi_pair[30]: num [1:500] -1.51 -1.51 -1.51 -1.51 -1.51 ...
#> .. .. .. ..$ lxi_pair[31]: num [1:500] -1.34 -1.34 -1.34 -1.34 -1.35 ...
#> .. .. .. ..$ lxi_pair[32]: num [1:500] -1.45 -1.45 -1.45 -1.45 -1.36 ...
#> .. .. .. ..$ lxi_pair[33]: num [1:500] -1.68 -1.68 -1.68 -1.68 -1.55 ...
#> .. .. .. ..$ lxi_pair[34]: num [1:500] -1.28 -1.28 -1.28 -1.28 -1.26 ...
#> .. .. .. ..$ lxi_pair[35]: num [1:500] -2.26 -2.26 -2.26 -2.26 -2.18 ...
#> .. .. .. ..$ lxi_pair[36]: num [1:500] -2.57 -2.57 -2.57 -2.57 -2.08 ...
#> .. .. .. ..$ lxi_pair[37]: num [1:500] -1.11 -1.11 -1.11 -1.11 -1.22 ...
#> .. .. .. ..$ lxi_pair[38]: num [1:500] -0.937 -0.937 -0.937 -0.937 -1.06 ...
#> .. .. .. ..$ lxi_pair[39]: num [1:500] -1.05 -1.05 -1.05 -1.05 -1.07 ...
#> .. .. .. ..$ lxi_pair[40]: num [1:500] -1.28 -1.28 -1.28 -1.28 -1.26 ...
#> .. .. .. ..$ lxi_pair[41]: num [1:500] -0.881 -0.881 -0.881 -0.881 -0.964 ...
#> .. .. .. ..$ lxi_pair[42]: num [1:500] -1.86 -1.86 -1.86 -1.86 -1.88 ...
#> .. .. .. ..$ lxi_pair[43]: num [1:500] -3.56 -3.56 -3.56 -3.56 -3 ...
#> .. .. .. .. [list output truncated]
#> .. .. .. ..- attr(*, "test_grad")= logi FALSE
#> .. .. .. ..- attr(*, "args")=List of 16
#> .. .. .. .. ..$ append_samples : logi FALSE
#> .. .. .. .. ..$ chain_id : num 1
#> .. .. .. .. ..$ control :List of 12
#> .. .. .. .. ..$ adapt_delta : num 0.8
#> .. .. .. .. ..$ adapt_engaged : logi TRUE
#> .. .. .. .. ..$ adapt_gamma : num 0.05
#> .. .. .. .. ..$ adapt_init_buffer: num 75
#> .. .. .. .. ..$ adapt_kappa : num 0.75
#> .. .. .. .. ..$ adapt_t0 : num 10
#> .. .. .. .. ..$ adapt_term_buffer: num 50
#> .. .. .. .. ..$ adapt_window : num 25
#> .. .. .. .. ..$ max_treedepth : int 10
#> .. .. .. .. ..$ metric : chr "diag_e"
#> .. .. .. .. ..$ stepsize : num 1
#> .. .. .. .. ..$ stepsize_jitter : num 0
#> .. .. .. .. ..$ enable_random_init: logi TRUE
#> .. .. .. .. ..$ init : chr "random"
#> .. .. .. .. ..$ init_list : NULL
#> .. .. .. .. ..$ init_radius : num 2
#> .. .. .. .. ..$ iter : int 500
#> .. .. .. .. ..$ method : chr "sampling"
#> .. .. .. .. ..$ random_seed : chr "42"
#> .. .. .. .. ..$ refresh : int 50

```

```

#> ..$ sampler_t      : chr "NUTS(diag_e)"
#> ..$ save_warmup    : logi TRUE
#> ..$ test_grad      : logi FALSE
#> ..$ thin           : int 1
#> ..$ warmup         : int 250
#> ..$ attr(*, "inits")= num [1:155] 6.296 0.174 3.545 5.554 0.161 ...
#> ..$ attr(*, "mean_pars")= num [1:155] 0.2271 6.2514 0.0589 4.9258 0.2899 ...
#> ..$ attr(*, "mean_lp__")= num -250
#> ..$ attr(*, "adaptation_info")= chr "# Adaptation terminated\n# Step size = 0.00953822\n#
#> ..$ attr(*, "elapsed_time")= Named num [1:2] 4.15 2.72
#> ..$ attr(*, "names")= chr [1:2] "warmup" "sample"
#> ..$ attr(*, "sampler_params")=List of 6
#> ..$ accept_stat__ : num [1:500] 1 0 0 0 1 ...
#> ..$ stepsize__    : num [1:500] 0.0625 14.3855 2.4312 0.2398 0.0186 ...
#> ..$ treedepth__   : num [1:500] 7 0 0 0 2 8 9 9 10 10 ...
#> ..$ n_leapfrog__  : num [1:500] 127 1 1 1 3 ...
#> ..$ divergent__   : num [1:500] 0 1 1 1 0 0 0 0 0 0 ...
#> ..$ energy__      : num [1:500] 1730 1177 1174 1181 1165 ...
#> ..$ attr(*, "return_code")= int 0
#> ..$ iter          : num 500
#> ..$ thin          : num 1
#> ..$ warmup        : num 250
#> ..$ chains        : num 1
#> ..$ n_save        : num 500
#> ..$ warmup2       : num 250
#> ..$ permutation:List of 1
#> ..$ : int [1:250] 104 3 58 225 42 24 158 43 143 150 ...
#> ..$ pars_oi       : chr [1:6] "lambda" "xi" "lxi_pair" "betav" ...
#> ..$ dims_oi       :List of 6
#> ..$ lambda        : num 49
#> ..$ xi            : num 7
#> ..$ lxi_pair      : num 49
#> ..$ betav         : num 49
#> ..$ beta          : num(0)
#> ..$ lp__          : num(0)
#> ..$ fnames_oi     : chr [1:156] "lambda[1]" "lambda[2]" "lambda[3]" "lambda[4]" ...
#> ..$ n_flatnames: int 156
#> ..@ inits         :List of 1
#> ..$ :List of 5
#> ..$ lambda        : num [1:49(1d)] 6.296 0.174 3.545 5.554 0.161 ...
#> ..$ xi            : num [1:7(1d)] 0.869 0.181 0.379 0.698 0.678 ...
#> ..$ lxi_pair      : num [1:49(1d)] -0.28 -1.85 -1.109 -0.499 -0.529 ...
#> ..$ betav         : num [1:49(1d)] 0.323 6.359 2.031 1.648 0.697 ...
#> ..$ beta          : num 0.00358
#> ..@ stan_args :List of 1
#> ..$ :List of 10
#> ..$ chain_id      : int 1
#> ..$ iter          : int 500
#> ..$ thin          : int 1
#> ..$ seed          : int 42
#> ..$ warmup        : num 250
#> ..$ init          : chr "random"
#> ..$ algorithm     : chr "NUTS"

```



```

#> .. .. .$ check_unknown_args: logi FALSE
#> .. .. .$ method : chr "sampling"
#> .. .. .$ control :List of 2
#> .. .. .$ adapt_delta : num 0.8
#> .. .. .$ max_treedepth: num 10
#> ..@ stanmodel :Formal class 'stanmodel' [package "rstan"] with 5 slots
#> .. .. .@ model_name : chr "gamma"
#> .. .. .@ model_code : chr "data {\n int<lower=1> N; // number of observations\n int Y[N]; //
#> .. .. .- attr(*, "model_name2")= chr "gamma"
#> .. .. .@ model_cpp :List of 2
#> .. .. . .$ model_cppname: chr "model44d73288805_gamma"
#> .. .. . .$ model_cppcode: chr "// Code generated by Stan version 2.19.1\n\n#include <stan/model/
#> .. .. .@ mk_cppmodule:function (object)
#> .. .. .@ dso :Formal class 'cxxdso' [package "rstan"] with 7 slots
#> .. .. . . .@ sig :List of 1
#> .. .. . . . .$ file44d4b554db5: chr(0)
#> .. .. . . .@ dso_saved : logi TRUE
#> .. .. . . .@ dso_filename: chr "file44d4b554db5"
#> .. .. . . .@ modulename : chr "stan_fit4model44d73288805_gamma_mod"
#> .. .. . . .@ system : chr "x86_64, darwin15.6.0"
#> .. .. . . .@ cxxflags : chr "CXXFLAGS=-isysroot /Library/Developer/CommandLineTools/SDKs/Mac
#> .. .. . . .@ .CXXDSOMISC :<environment: 0x7fc7548377f0>
#> ..@ date : chr "Fri Jan 8 10:22:05 2021"
#> ..@ .MISC :<environment: 0x7fc74cfd960>
str(ans.gp)
#> Formal class 'stanfit' [package "rstan"] with 10 slots
#> ..@ model_name: chr "gp"
#> ..@ model_pars: chr [1:11] "rho" "alpha" "mu" "beta" ...
#> ..@ par_dims :List of 11
#> .. .. .$ rho : num 2
#> .. .. .$ alpha : num(0)
#> .. .. .$ mu : num(0)
#> .. .. .$ beta : num 900
#> .. .. .$ xi : num 7
#> .. .. .$ f : num 49
#> .. .. .$ xi1 : num 49
#> .. .. .$ xi2 : num 49
#> .. .. .$ diagSPD : num 900
#> .. .. .$ SPD_beta: num 900
#> .. .. .$ lp_ : num(0)
#> ..@ mode : int 0
#> ..@ sim :List of 12
#> .. .. .$ samples :List of 1
#> .. .. . .$ :List of 2859
#> .. .. . . .$ rho[1] : num [1:500] 3.4 3.4 3.4 3.4 3.79 ...
#> .. .. . . .$ rho[2] : num [1:500] 18.26 18.26 18.26 18.26 1.13 ...
#> .. .. . . .$ alpha : num [1:500] 0.9858 0.9858 0.9858 0.9858 0.0248 ...
#> .. .. . . .$ mu : num [1:500] -1.37 -1.37 -1.37 -1.37 0.798 ...
#> .. .. . . .$ beta[1] : num [1:500] -1.474 -1.474 -1.474 -1.474 0.135 ...
#> .. .. . . .$ beta[2] : num [1:500] 1.346 1.346 1.346 1.346 -0.477 ...
#> .. .. . . .$ beta[3] : num [1:500] -1.561 -1.561 -1.561 -1.561 0.279 ...
#> .. .. . . .$ beta[4] : num [1:500] 0.175 0.175 0.175 0.175 0.374 ...
#> .. .. . . .$ beta[5] : num [1:500] -0.877 -0.877 -0.877 -0.877 -0.233 ...

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#> .. .. .. ..$ beta[6] : num [1:500] 0.0607 0.0607 0.0607 0.0607 0.3915 ...
#> .. .. .. ..$ beta[7] : num [1:500] -0.11 -0.11 -0.11 -0.11 0.416 ...
#> .. .. .. ..$ beta[8] : num [1:500] -0.394 -0.394 -0.394 -0.394 -0.139 ...
#> .. .. .. ..$ beta[9] : num [1:500] 0.639 0.639 0.639 0.639 -0.607 ...
#> .. .. .. ..$ beta[10] : num [1:500] -1.472 -1.472 -1.472 -1.472 0.624 ...
#> .. .. .. ..$ beta[11] : num [1:500] 0.53 0.53 0.53 0.53 1.45 ...
#> .. .. .. ..$ beta[12] : num [1:500] -0.66 -0.66 -0.66 -0.66 0.333 ...
#> .. .. .. ..$ beta[13] : num [1:500] -0.848 -0.848 -0.848 -0.848 1.204 ...
#> .. .. .. ..$ beta[14] : num [1:500] -0.81 -0.81 -0.81 -0.81 -1.1 ...
#> .. .. .. ..$ beta[15] : num [1:500] -0.351 -0.351 -0.351 -0.351 1.496 ...
#> .. .. .. ..$ beta[16] : num [1:500] 0.181 0.181 0.181 0.181 -1.027 ...
#> .. .. .. ..$ beta[17] : num [1:500] 0.803 0.803 0.803 0.803 -0.675 ...
#> .. .. .. ..$ beta[18] : num [1:500] -1.12 -1.12 -1.12 -1.12 1.65 ...
#> .. .. .. ..$ beta[19] : num [1:500] 0.525 0.525 0.525 0.525 -0.638 ...
#> .. .. .. ..$ beta[20] : num [1:500] -1.242 -1.242 -1.242 -1.242 0.242 ...
#> .. .. .. ..$ beta[21] : num [1:500] 1.0644 1.0644 1.0644 1.0644 -0.0206 ...
#> .. .. .. ..$ beta[22] : num [1:500] -0.188 -0.188 -0.188 -0.188 0.414 ...
#> .. .. .. ..$ beta[23] : num [1:500] 1.2935 1.2935 1.2935 1.2935 -0.0175 ...
#> .. .. .. ..$ beta[24] : num [1:500] -0.87 -0.87 -0.87 -0.87 1.63 ...
#> .. .. .. ..$ beta[25] : num [1:500] -0.207 -0.207 -0.207 -0.207 0.974 ...
#> .. .. .. ..$ beta[26] : num [1:500] -0.873 -0.873 -0.873 -0.873 -0.355 ...
#> .. .. .. ..$ beta[27] : num [1:500] 0.366 0.366 0.366 0.366 -0.922 ...
#> .. .. .. ..$ beta[28] : num [1:500] 0.924 0.924 0.924 0.924 -0.213 ...
#> .. .. .. ..$ beta[29] : num [1:500] 1.93 1.93 1.93 1.93 -1.37 ...
#> .. .. .. ..$ beta[30] : num [1:500] -1.58 -1.58 -1.58 -1.58 0.371 ...
#> .. .. .. ..$ beta[31] : num [1:500] 0.525 0.525 0.525 0.525 -1.301 ...
#> .. .. .. ..$ beta[32] : num [1:500] -0.696 -0.696 -0.696 -0.696 2.018 ...
#> .. .. .. ..$ beta[33] : num [1:500] 1.15 1.15 1.15 1.15 -0.41 ...
#> .. .. .. ..$ beta[34] : num [1:500] 0.549 0.549 0.549 0.549 -0.268 ...
#> .. .. .. ..$ beta[35] : num [1:500] 1.28 1.28 1.28 1.28 -0.297 ...
#> .. .. .. ..$ beta[36] : num [1:500] -0.0654 -0.0654 -0.0654 -0.0654 -0.0625 ...
#> .. .. .. ..$ beta[37] : num [1:500] -0.748 -0.748 -0.748 -0.748 0.325 ...
#> .. .. .. ..$ beta[38] : num [1:500] -0.0852 -0.0852 -0.0852 -0.0852 0.6309 ...
#> .. .. .. ..$ beta[39] : num [1:500] 1.68 1.68 1.68 1.68 -1.76 ...
#> .. .. .. ..$ beta[40] : num [1:500] 0.18 0.18 0.18 0.18 -0.397 ...
#> .. .. .. ..$ beta[41] : num [1:500] -1.117 -1.117 -1.117 -1.117 0.734 ...
#> .. .. .. ..$ beta[42] : num [1:500] -0.58924 -0.58924 -0.58924 -0.58924 -0.00853 ...
#> .. .. .. ..$ beta[43] : num [1:500] 1.023 1.023 1.023 1.023 0.107 ...
#> .. .. .. ..$ beta[44] : num [1:500] -1.096 -1.096 -1.096 -1.096 0.331 ...
#> .. .. .. ..$ beta[45] : num [1:500] -0.927 -0.927 -0.927 -0.927 0.0104 ...
#> .. .. .. ..$ beta[46] : num [1:500] 0.946 0.946 0.946 0.946 -1.534 ...
#> .. .. .. ..$ beta[47] : num [1:500] -1 -1 -1 -1 -1.55 ...
#> .. .. .. ..$ beta[48] : num [1:500] 0.212 0.212 0.212 0.212 -0.637 ...
#> .. .. .. ..$ beta[49] : num [1:500] 1.35 1.35 1.35 1.35 -1.51 ...
#> .. .. .. ..$ beta[50] : num [1:500] 0.302 0.302 0.302 0.302 -0.91 ...
#> .. .. .. ..$ beta[51] : num [1:500] 0.0957 0.0957 0.0957 0.0957 -0.3205 ...
#> .. .. .. ..$ beta[52] : num [1:500] 2.127 2.127 2.127 2.127 -0.976 ...
#> .. .. .. ..$ beta[53] : num [1:500] 1.42 1.42 1.42 1.42 -0.208 ...
#> .. .. .. ..$ beta[54] : num [1:500] -1.354 -1.354 -1.354 -1.354 0.626 ...
#> .. .. .. ..$ beta[55] : num [1:500] -0.153 -0.153 -0.153 -0.153 -0.97 ...
#> .. .. .. ..$ beta[56] : num [1:500] 0.793 0.793 0.793 0.793 -1.816 ...
#> .. .. .. ..$ beta[57] : num [1:500] 1.62 1.62 1.62 1.62 -1.98 ...
#> .. .. .. ..$ beta[58] : num [1:500] 0.0437 0.0437 0.0437 0.0437 -0.4259 ...

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#> .. .. .. ..$ beta[59] : num [1:500] 0.4087 0.4087 0.4087 0.4087 0.0947 ...
#> .. .. .. ..$ beta[60] : num [1:500] -0.576 -0.576 -0.576 -0.576 1.098 ...
#> .. .. .. ..$ beta[61] : num [1:500] -0.455 -0.455 -0.455 -0.455 0.603 ...
#> .. .. .. ..$ beta[62] : num [1:500] 0.0348 0.0348 0.0348 0.0348 -1.8896 ...
#> .. .. .. ..$ beta[63] : num [1:500] 0.46 0.46 0.46 0.46 0.553 ...
#> .. .. .. ..$ beta[64] : num [1:500] -0.521 -0.521 -0.521 -0.521 0.329 ...
#> .. .. .. ..$ beta[65] : num [1:500] -0.2196 -0.2196 -0.2196 -0.2196 0.0413 ...
#> .. .. .. ..$ beta[66] : num [1:500] -0.859 -0.859 -0.859 -0.859 1.33 ...
#> .. .. .. ..$ beta[67] : num [1:500] 0.704 0.704 0.704 0.704 -0.328 ...
#> .. .. .. ..$ beta[68] : num [1:500] 1.192 1.192 1.192 1.192 -0.624 ...
#> .. .. .. ..$ beta[69] : num [1:500] -1.146 -1.146 -1.146 -1.146 0.707 ...
#> .. .. .. ..$ beta[70] : num [1:500] -2.18 -2.18 -2.18 -2.18 0.542 ...
#> .. .. .. ..$ beta[71] : num [1:500] 1.107 1.107 1.107 1.107 0.418 ...
#> .. .. .. ..$ beta[72] : num [1:500] 0.546 0.546 0.546 0.546 -0.735 ...
#> .. .. .. ..$ beta[73] : num [1:500] -1.11 -1.11 -1.11 -1.11 -0.356 ...
#> .. .. .. ..$ beta[74] : num [1:500] -0.7032 -0.7032 -0.7032 -0.7032 0.0456 ...
#> .. .. .. ..$ beta[75] : num [1:500] -0.584 -0.584 -0.584 -0.584 0.79 ...
#> .. .. .. ..$ beta[76] : num [1:500] -0.864 -0.864 -0.864 -0.864 1.895 ...
#> .. .. .. ..$ beta[77] : num [1:500] -1.034 -1.034 -1.034 -1.034 0.525 ...
#> .. .. .. ..$ beta[78] : num [1:500] 1.437 1.437 1.437 1.437 0.109 ...
#> .. .. .. ..$ beta[79] : num [1:500] 1.8425 1.8425 1.8425 1.8425 0.0713 ...
#> .. .. .. ..$ beta[80] : num [1:500] -0.724 -0.724 -0.724 -0.724 -1.365 ...
#> .. .. .. ..$ beta[81] : num [1:500] -1.09 -1.09 -1.09 -1.09 1.69 ...
#> .. .. .. ..$ beta[82] : num [1:500] -0.995 -0.995 -0.995 -0.995 0.501 ...
#> .. .. .. ..$ beta[83] : num [1:500] -0.43799 -0.43799 -0.43799 -0.43799 -0.00252 ...
#> .. .. .. ..$ beta[84] : num [1:500] -0.6469 -0.6469 -0.6469 -0.6469 0.00802 ...
#> .. .. .. ..$ beta[85] : num [1:500] -0.423 -0.423 -0.423 -0.423 0.156 ...
#> .. .. .. ..$ beta[86] : num [1:500] -0.618 -0.618 -0.618 -0.618 0.188 ...
#> .. .. .. ..$ beta[87] : num [1:500] 0.626 0.626 0.626 0.626 -1.395 ...
#> .. .. .. ..$ beta[88] : num [1:500] 0.265 0.265 0.265 0.265 -0.758 ...
#> .. .. .. ..$ beta[89] : num [1:500] 0.461 0.461 0.461 0.461 -0.367 ...
#> .. .. .. ..$ beta[90] : num [1:500] -0.614 -0.614 -0.614 -0.614 -1.164 ...
#> .. .. .. ..$ beta[91] : num [1:500] 0.0788 0.0788 0.0788 0.0788 -1.2827 ...
#> .. .. .. ..$ beta[92] : num [1:500] -1.08 -1.08 -1.08 -1.08 3.02 ...
#> .. .. .. ..$ beta[93] : num [1:500] -1.79 -1.79 -1.79 -1.79 2.11 ...
#> .. .. .. ..$ beta[94] : num [1:500] -1.55 -1.55 -1.55 -1.55 1.46 ...
#> .. .. .. ..$ beta[95] : num [1:500] 2.29 2.29 2.29 2.29 -0.214 ...
#> .. .. .. .. [list output truncated]
#> .. .. .. ..- attr(*, "test_grad")= logi FALSE
#> .. .. .. ..- attr(*, "args")=List of 16
#> .. .. .. .. ..$ append_samples : logi FALSE
#> .. .. .. .. ..$ chain_id : num 1
#> .. .. .. .. ..$ control :List of 12
#> .. .. .. .. ..$ adapt_delta : num 0.8
#> .. .. .. .. ..$ adapt_engaged : logi TRUE
#> .. .. .. .. ..$ adapt_gamma : num 0.05
#> .. .. .. .. ..$ adapt_init_buffer: num 75
#> .. .. .. .. ..$ adapt_kappa : num 0.75
#> .. .. .. .. ..$ adapt_t0 : num 10
#> .. .. .. .. ..$ adapt_term_buffer: num 50
#> .. .. .. .. ..$ adapt_window : num 25
#> .. .. .. .. ..$ max_treedepth : int 10
#> .. .. .. .. ..$ metric : chr "diag_e"

```

```

#> ..$ stepsize : num 1
#> ..$ stepsize_jitter : num 0
#> ..$ enable_random_init: logi TRUE
#> ..$ init : chr "random"
#> ..$ init_list : NULL
#> ..$ init_radius : num 2
#> ..$ iter : int 500
#> ..$ method : chr "sampling"
#> ..$ random_seed : chr "42"
#> ..$ refresh : int 50
#> ..$ sampler_t : chr "NUTS(diag_e)"
#> ..$ save_warmup : logi TRUE
#> ..$ test_grad : logi FALSE
#> ..$ thin : int 1
#> ..$ warmup : int 250
#> ..- attr(*, "inits")= num [1:2858] 6.296 0.174 3.545 1.715 -1.829 ...
#> ..- attr(*, "mean_pars")= num [1:2858] 10.2915 6.7725 4.0213 -2.6167 0.0371 ...
#> ..- attr(*, "mean_lp__")= num -11822
#> ..- attr(*, "adaptation_info")= chr "# Adaptation terminated\n# Step size = 0.0460635\n#
#> ..- attr(*, "elapsed_time")= Named num [1:2] 49.3 41.9
#> ..- attr(*, "names")= chr [1:2] "warmup" "sample"
#> ..- attr(*, "sampler_params")=List of 6
#> ..$ accept_stat__ : num [1:500] 0.722 0 0 0 0.949 ...
#> ..$ stepsize__ : num [1:500] 0.0625 8.6813 1.26319 0.11439 0.00842 ...
#> ..$ treedepth__ : num [1:500] 4 0 0 0 9 9 8 7 7 6 ...
#> ..$ n_leapfrog__ : num [1:500] 18 1 1 1 511 511 255 127 127 63 ...
#> ..$ divergent__ : num [1:500] 1 1 1 1 0 0 0 0 0 0 ...
#> ..$ energy__ : num [1:500] 14123 13331 13260 13318 13301 ...
#> ..- attr(*, "return_code")= int 0
#> ..$ iter : num 500
#> ..$ thin : num 1
#> ..$ warmup : num 250
#> ..$ chains : num 1
#> ..$ n_save : num 500
#> ..$ warmup2 : num 250
#> ..$ permutation:List of 1
#> ..$ : int [1:250] 187 213 108 149 198 47 105 202 88 114 ...
#> ..$ pars_oi : chr [1:11] "rho" "alpha" "mu" "beta" ...
#> ..$ dims_oi :List of 11
#> ..$ rho : num 2
#> ..$ alpha : num(0)
#> ..$ mu : num(0)
#> ..$ beta : num 900
#> ..$ xi : num 7
#> ..$ f : num 49
#> ..$ xi1 : num 49
#> ..$ xi2 : num 49
#> ..$ diagSPD : num 900
#> ..$ SPD_beta: num 900
#> ..$ lp__ : num(0)
#> ..$ fnames_oi : chr [1:2859] "rho[1]" "rho[2]" "alpha" "mu" ...
#> ..$ n_flatnames: int 2859
#> ..@ inits :List of 1

```

```

#> .. ..$ :List of 10
#> .. ..$ rho : num [1:2(1d)] 6.296 0.174
#> .. ..$ alpha : num 3.54
#> .. ..$ mu : num 1.71
#> .. ..$ beta : num [1:900(1d)] -1.829 1.765 -1.811 -0.796 -1.406 ...
#> .. ..$ xi : num [1:7(1d)] 0.831 0.278 0.714 0.583 0.655 ...
#> .. ..$ f : num [1:49(1d)] -0.872 -1.043 -2.267 -2.939 -1.625 ...
#> .. ..$ xi1 : num [1:49(1d)] 0.831 0.278 0.714 0.583 0.655 ...
#> .. ..$ xi2 : num [1:49(1d)] 0.831 0.831 0.831 0.831 0.831 ...
#> .. ..$ diagSPD : num [1:900(1d)] 9.24 9.24 9.24 9.24 9.24 ...
#> .. ..$ SPD_beta: num [1:900(1d)] -16.9 16.31 -16.74 -7.36 -13 ...
#> ..@ stan_args :List of 1
#> .. ..$ :List of 10
#> .. ..$ chain_id : int 1
#> .. ..$ iter : int 500
#> .. ..$ thin : int 1
#> .. ..$ seed : int 42
#> .. ..$ warmup : num 250
#> .. ..$ init : chr "random"
#> .. ..$ algorithm : chr "NUTS"
#> .. ..$ check_unknown_args: logi FALSE
#> .. ..$ method : chr "sampling"
#> .. ..$ control :List of 2
#> .. ..$ adapt_delta : num 0.8
#> .. ..$ max_treedepth: num 10
#> ..@ stanmodel :Formal class 'stanmodel' [package "rstan"] with 5 slots
#> .. ..@ model_name : chr "gp"
#> .. ..@ model_code : chr "functions {\n vector lambda_nD(real[] L, int[] m, int D) {\n vect
#> .. ..$- attr(*, "model_name2")= chr "gp"
#> .. ..@ model_cpp :List of 2
#> .. ..$ model_cppname: chr "model44de1fe86a_gp"
#> .. ..$ model_cppcode: chr "// Code generated by Stan version 2.19.1\n\n#include <stan/model/
#> .. ..@ mk_cppmodule:function (object)
#> .. ..@ dso :Formal class 'cxxdso' [package "rstan"] with 7 slots
#> .. ..$ sig :List of 1
#> .. ..$ file44d57a56cda: chr(0)
#> .. ..@ dso_saved : logi TRUE
#> .. ..@ dso_filename: chr "file44d57a56cda"
#> .. ..@ modulename : chr "stan_fit4model44de1fe86a_gp_mod"
#> .. ..@ system : chr "x86_64, darwin15.6.0"
#> .. ..@ cxxflags : chr "CXXFLAGS=-isysroot /Library/Developer/CommandLineTools/SDKs/Mac
#> .. ..@ .CXXDSOMISC :<environment: 0x7fc76227edd0>
#> ..@ date : chr "Fri Jan 8 10:24:51 2021"
#> ..@ .MISC :<environment: 0x7fc7613eece0>

```

We are mostly interested in the marginal posterior distribution

$$p(\pi|n),$$

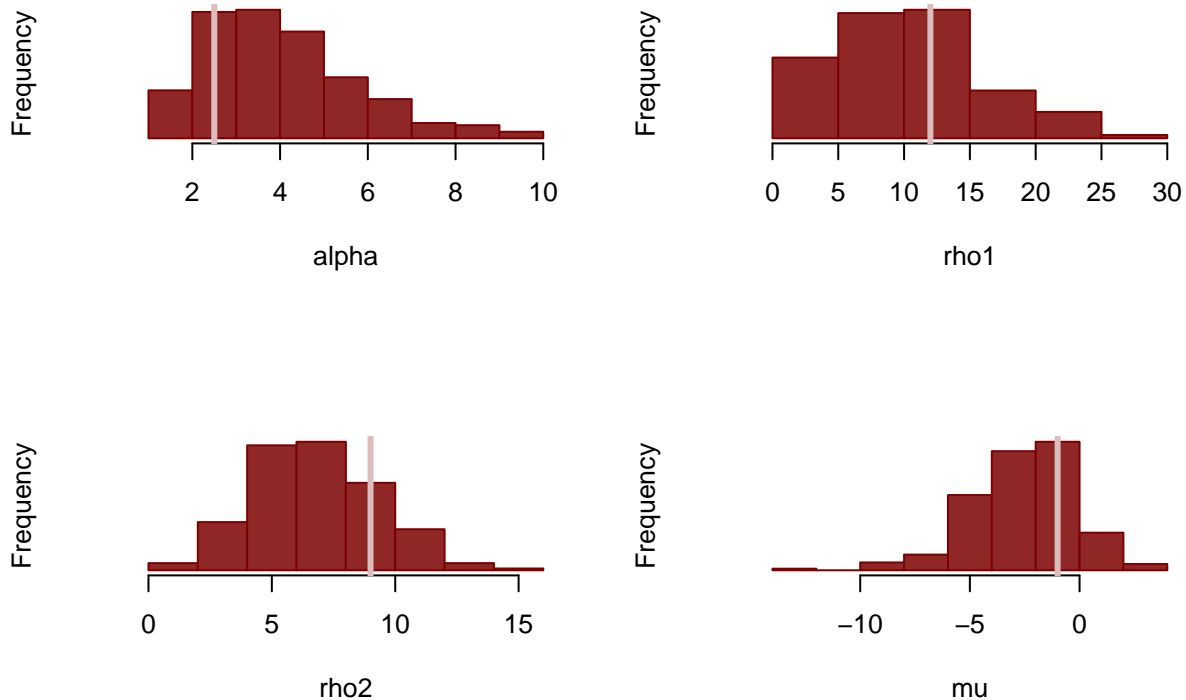
and the algorithm returns samples of the log Poisson rates  $\log \lambda$ , from which the transmission flows  $\pi$  can be calculated.

In addition, estimated parameters can be compared with the true hyperparameter values.

```

params_gamma <- extract(ans.gamma)
params_gp <- extract(ans.gp)
c_light <- c("#DCBCBC")
c_dark <- c("#8F2727")
c_dark_highlight <- c("#7C0000")
par(mfrow=c(2, 2))
hist(params_gp$alpha, main="", xlab="alpha", col=c_dark, border=c_dark_highlight, yaxt='n')
abline(v=2.5, col=c_light, lty=1, lwd=3)
hist(params_gp$rho[,1], main="", xlab="rho1", col=c_dark, border=c_dark_highlight, yaxt='n')
abline(v=12, col=c_light, lty=1, lwd=3)
hist(params_gp$rho[,2], main="", xlab="rho2", col=c_dark, border=c_dark_highlight, yaxt='n')
abline(v=9, col=c_light, lty=1, lwd=3)
hist(params_gp$mu, main="", xlab="mu", col=c_dark, border=c_dark_highlight, yaxt='n')
abline(v=-1, col=c_light, lty=1, lwd=3)

```



That's it for now. Of course we would like to run the MCMC chain for longer, perhaps 10,000 steps. To check for convergence, calculate effective sample sizes, and quantiles of the posterior distribution, have a look at the other vignettes.